

Homework

CALC OK: For $0 \leq t \leq 31$, the rate of change of the number of mosquitoes on Tropical Island at time t days is modeled by $R(t) = 5t \cos(t^5)$ mosquitoes per day. There are 1000 mosquitoes on Tropical Island at time $t=0$.

- a. Show that the number of mosquitoes is increasing at time $t=6$.

$$R(6) = 5(6) \cos(30) = 4.627 \text{ or } 4.628 \text{ mosquitoes/day}$$

$R(6)$ is positive, so the number of mosquitoes is increasing.

derivative of $R(t)$

- b. At time $t=6$, is the number of mosquitoes increasing at an increasing rate, or is the number of mosquitoes increasing at a decreasing rate? Give a reason for your answer.

$$R'(t) = 5 + (-\sin(5t) \cdot 5) + 5 \cos(5t)$$

$$R'(6) = -30 \sin(30) \cdot 5 + 5 \cos(30) = 148.976 \text{ mosquitoes/day}^2$$

if you have a calculator, jump straight here.

The number of mosquitoes is increasing at an increasing rate b/c $R'(6)$ is positive. That means $R(t)$, the rate of change of mosquitoes is increasing. $R(6)$ is positive [# of mosquitoes is increasing]. That means $R'(6)$ being positive shows $\underbrace{R(t)}_{\text{the population}}$ is increasing at an increasing rate.

NO CALC: People are entering a building at a rate modeled by $f(t)$ people per hour and exiting the building at a rate modeled by $g(t)$ people per hour, where t is measured in hours. The functions f and g are nonnegative and differentiable for all times t . Write an inequality that indicates that the rate of change of the number of people in the building is increasing at time t ?

use both enter and exit rate

$$f(t) - g(t) > 0$$

b/c if $f(t) - g(t)$ is positive, overall the # of people in the building is increasing (in other words, rate in $>$ rate out)

HW: Watch the Three videos on Related Rates and take notes. SUPER IMPORTANT!